

## ADVANCED SUBSIDIARY GCE MATHEMATICS

**Core Mathematics 1** 

WEDNESDAY 9 JANUARY 2008

4721/01

Afternoon

Time: 1 hour 30 minutes

Additional materials: Answer Booklet (8 pages) List of Formulae (MF1)

## INSTRUCTIONS TO CANDIDATES

- Write your name, centre number and candidate number in the spaces provided on the answer booklet.
- Read each question carefully and make sure you know what you have to do before starting your answer.
- Answer **all** the questions.
- Give non-exact numerical answers correct to 3 significant figures unless a different degree of accuracy is specified in the question or is clearly appropriate.
- You are not permitted to use a calculator in this paper.

## **INFORMATION FOR CANDIDATES**

- The number of marks is given in brackets [] at the end of each question or part question.
- The total number of marks for this paper is 72.
- You are reminded of the need for clear presentation in your answers.



You are not allowed to use a calculator in this paper.

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PMT

1 Express 
$$\frac{4}{3-\sqrt{7}}$$
 in the form  $a + b\sqrt{7}$ , where *a* and *b* are integers. [3]

- 2 (i) Write down the equation of the circle with centre (0, 0) and radius 7. [1]
  - (ii) A circle with centre (3, 5) has equation  $x^2 + y^2 6x 10y 30 = 0$ . Find the radius of the circle. [2]
- 3 Given that  $3x^2 + bx + 10 = a(x+3)^2 + c$  for all values of x, find the values of the constants a, b and c. [4]
- 4 Solve the equations
  - (i)  $10^p = 0.1$ , [1]

(ii) 
$$(25k^2)^{\frac{1}{2}} = 15,$$
 [3]

(iii) 
$$t^{-\frac{1}{3}} = \frac{1}{2}$$
. [2]

- 5 (i) Sketch the curve  $y = x^3 + 2$ . [2]
  - (ii) Sketch the curve  $y = 2\sqrt{x}$ . [2]
  - (iii) Describe a transformation that transforms the curve  $y = 2\sqrt{x}$  to the curve  $y = 3\sqrt{x}$ . [3]

6 (i) Solve the equation  $x^2 + 8x + 10 = 0$ , giving your answers in simplified surd form. [3]

- (ii) Sketch the curve  $y = x^2 + 8x + 10$ , giving the coordinates of the point where the curve crosses the y-axis. [3]
- (iii) Solve the inequality  $x^2 + 8x + 10 \ge 0$ . [2]
- 7 (i) Find the gradient of the line *l* which has equation x + 2y = 4. [1]
  - (ii) Find the equation of the line parallel to l which passes through the point (6, 5), giving your answer in the form ax + by + c = 0, where a, b and c are integers. [3]
  - (iii) Solve the simultaneous equations

$$y = x^2 + x + 1$$
 and  $x + 2y = 4$ . [4]

[6]

[2]

(i) Find the coordinates of the stationary points on the curve  $y = x^3 + x^2 - x + 3$ .

- (ii) Determine whether each stationary point is a maximum point or a minimum point. [3]
- (iii) For what values of x does  $x^3 + x^2 x + 3$  decrease as x increases?

8

- 9 The points A and B have coordinates (-5, -2) and (3, 1) respectively.
  - (i) Find the equation of the line AB, giving your answer in the form ax + by + c = 0. [3]
  - (ii) Find the coordinates of the mid-point of *AB*. [2]
  - The point *C* has coordinates (-3, 4).
  - (iii) Calculate the length of *AC*, giving your answer in simplified surd form. [3]
  - (iv) Determine whether the line AC is perpendicular to the line BC, showing all your working. [4]

10 Given that 
$$f(x) = 8x^3 + \frac{1}{x^3}$$
,  
(i) find  $f''(x)$  [5]

(1) find 
$$f(x)$$
, [5]

(ii) solve the equation 
$$f(x) = -9$$
. [5]

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